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Since the level at $2^{n-1}$ at the bottom of the top triangle $T_{n-1}$ is full so the level $2^{n-1}+2$ will be full. When the generations have progressed to the bottoms of the four triangles $T_{n-2}$ none of the cells in the lower diamond $D$ are ON. Also, none of the levels in the upper half of the diamond $D$ will become full since the diagonal bottoms of the two inner triangles $T_{n-2}$ that meet at the center at level $2^{n-1}$ are full sections so that their adjacent sections inside diamond D will stay OFF. As the generations proceed down to the bottom level $2^{n}$ each level that is full in the bottom halves of the two lower companion triangles $T_{n-1}$ will be filled across the diamond D , so that their entire matching levels will be filled. Therefore, the lower half of triangle $T_{n}$ will have the additional $\mathrm{n}-1$ filled levels at:

$$
2^{n-1}+2,2^{n-1}+2+2^{n-2}, 2^{n-1}+2+2^{n-2}+2^{n-3}, \ldots, 2^{n-1}+2+\sum_{k=2}^{n-1} 2^{n-k}=2^{n} .
$$

