Integers $\boldsymbol{n}$ that are $\boldsymbol{k}$-powerful. Compiled by Stan Wagon, Jan. 2019.
For $k=5$ : see A323610; $k=6$ : see A323629; $k=7$ : see A323614.

|  | smaller than critical power of 2 | $2^{k+1}$ |  |  |  |  |  |  |  |  |  |  | differences $\Delta$ | notes |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $k=-1$ |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | $\rightarrow \infty$ | 1 | symmetric |
| $k=0$ |  | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 | 20 | $\rightarrow \infty$ | 2 | antisymmetric |
| $k=1$ |  | 4 | 8 | 12 | 16 | 20 | 24 | 28 | 32 | 36 | 40 | $\rightarrow \infty$ | 4 | symmetric |
| $k=2$ |  | $\underline{8}$ | 12 | 16 | 20 | 24 | 28 | 32 | 36 | 40 | 44 | $\rightarrow \infty$ | 4 | antisymmetric |
| $k=3$ |  | 16 | 24 | 32 | 40 | 48 | 56 | 64 | 72 | 80 | 88 | $\rightarrow \infty$ | 8 | symmetric |
| $k=4$ |  | 32 | 40 | 48 | $\overline{56}$ | 64 | 72 | 80 | 88 | 96 | 104 | $\rightarrow \infty$ | 8 | antisymmetric |
| $k=5$ | 48 | $\overline{64}$ | $\overline{72}$ | $\overline{\mathbf{8 0}}$ | 88 | 96 | 104 | 112 | 120 | 128 | 136 | $\rightarrow \infty$ | 8 | symmetric |
| $k=6$ | $\overline{96}$ | $\overline{128}$ | 144 | 160 | 176 | 192 | 200 | 208 | 216 | 224 | 232 | $\rightarrow \infty$ | 8 | antisymmetric |
| $k=7$ | $\overline{144} \overline{192} 208224240$ | $\overline{256}$ | 272 | 288 | 304 | 320 | 336 | 352 | 368 | 384 | 400 | $\rightarrow \infty$ | 16 | symmetric |
| $k=8$ | 192 | $\overline{512}$ | 544 |  |  |  |  |  |  |  |  |  | $16 ?$ | antisymmetric? 256 fails |

Red entries are those that are not part of the ultimate arithmetic progression that holds out to infinity. Underlined entries admit a unique witnessing set. Overlined entries are not unique (and many of the unmarked ones are not unique). Essentially nothing is known about $k=8$, though it is known that 192 is the smallest example. The discoverers of the final complete sequence are:

```
k=2 and 3: David Boyd
\(k=4\) and 5: Berend and Golan
\(k=6\) and 7 : Golan, Pratt, and Wagon
```

Some of the negative results for $k=6$ and 7 are by Berend and Golan.

