

**There are 216 labeled 3-node T<sub>0</sub>-hypergraphs without multiple hyperedges  
(empty hyperedge included):**

(A hypergraph is a T<sub>0</sub> hypergraph if for every two distinct nodes there exists a hyperedge containing one but not the other node)

12 hypergraphs with 2 hyperedges:

- |    |                          |
|----|--------------------------|
| 1  | $\{\{3\}, \{2\}\}$       |
| 2  | $\{\{3\}, \{2, 3\}\}$    |
| 3  | $\{\{2\}, \{2, 3\}\}$    |
| 4  | $\{\{3\}, \{1\}\}$       |
| 5  | $\{\{3\}, \{1, 3\}\}$    |
| 6  | $\{\{2\}, \{1\}\}$       |
| 7  | $\{\{2, 3\}, \{1, 3\}\}$ |
| 8  | $\{\{2\}, \{1, 2\}\}$    |
| 9  | $\{\{2, 3\}, \{1, 2\}\}$ |
| 10 | $\{\{1\}, \{1, 3\}\}$    |
| 11 | $\{\{1\}, \{1, 2\}\}$    |
| 12 | $\{\{1, 3\}, \{1, 2\}\}$ |

44 hypergraphs with 3 hyperedges:

- |    |                                    |
|----|------------------------------------|
| 1  | $\{\{\}, \{3\}, \{2\}\}$           |
| 2  | $\{\{\}, \{3\}, \{2, 3\}\}$        |
| 3  | $\{\{\}, \{2\}, \{2, 3\}\}$        |
| 4  | $\{\{3\}, \{2\}, \{2, 3\}\}$       |
| 5  | $\{\{\}, \{3\}, \{1\}\}$           |
| 6  | $\{\{\}, \{3\}, \{1, 3\}\}$        |
| 7  | $\{\{\}, \{2\}, \{1\}\}$           |
| 8  | $\{\{\}, \{2, 3\}, \{1, 3\}\}$     |
| 9  | $\{\{3\}, \{2\}, \{1\}\}$          |
| 10 | $\{\{3\}, \{2\}, \{1, 3\}\}$       |
| 11 | $\{\{3\}, \{2, 3\}, \{1\}\}$       |
| 12 | $\{\{3\}, \{2, 3\}, \{1, 3\}\}$    |
| 13 | $\{\{\}, \{2\}, \{1, 2\}\}$        |
| 14 | $\{\{\}, \{2, 3\}, \{1, 2\}\}$     |
| 15 | $\{\{3\}, \{2\}, \{1, 2\}\}$       |
| 16 | $\{\{3\}, \{2\}, \{1, 2, 3\}\}$    |
| 17 | $\{\{3\}, \{2, 3\}, \{1, 2\}\}$    |
| 18 | $\{\{3\}, \{2, 3\}, \{1, 2, 3\}\}$ |
| 19 | $\{\{2\}, \{2, 3\}, \{1\}\}$       |
| 20 | $\{\{2\}, \{2, 3\}, \{1, 3\}\}$    |
| 21 | $\{\{2\}, \{2, 3\}, \{1, 2\}\}$    |
| 22 | $\{\{2\}, \{2, 3\}, \{1, 2, 3\}\}$ |
| 23 | $\{\{\}, \{1\}, \{1, 3\}\}$        |
| 24 | $\{\{3\}, \{1\}, \{1, 3\}\}$       |
| 25 | $\{\{\}, \{1\}, \{1, 2\}\}$        |
| 26 | $\{\{\}, \{1, 3\}, \{1, 2\}\}$     |
| 27 | $\{\{3\}, \{1\}, \{1, 2\}\}$       |

28  $\{\{3\}, \{1\}, \{1, 2, 3\}\}$   
 29  $\{\{3\}, \{1, 3\}, \{1, 2\}\}$   
 30  $\{\{3\}, \{1, 3\}, \{1, 2, 3\}\}$   
 31  $\{\{2\}, \{1\}, \{1, 3\}\}$   
 32  $\{\{2, 3\}, \{1\}, \{1, 3\}\}$   
 33  $\{\{2\}, \{1\}, \{1, 2\}\}$   
 34  $\{\{2\}, \{1\}, \{1, 2, 3\}\}$   
 35  $\{\{2\}, \{1, 3\}, \{1, 2\}\}$   
 36  $\{\{2, 3\}, \{1\}, \{1, 2\}\}$   
 37  $\{\{2, 3\}, \{1, 3\}, \{1, 2\}\}$   
 38  $\{\{2, 3\}, \{1, 3\}, \{1, 2, 3\}\}$   
 39  $\{\{2\}, \{1, 2\}, \{1, 2, 3\}\}$   
 40  $\{\{2, 3\}, \{1, 2\}, \{1, 2, 3\}\}$   
 41  $\{\{1\}, \{1, 3\}, \{1, 2\}\}$   
 42  $\{\{1\}, \{1, 3\}, \{1, 2, 3\}\}$   
 43  $\{\{1\}, \{1, 2\}, \{1, 2, 3\}\}$   
 44  $\{\{1, 3\}, \{1, 2\}, \{1, 2, 3\}\}$

67 hypergraphs with 4 hyperedges:

1  $\{\{\}, \{3\}, \{2\}, \{2, 3\}\}$   
 2  $\{\{\}, \{3\}, \{2\}, \{1\}\}$   
 3  $\{\{\}, \{3\}, \{2\}, \{1, 3\}\}$   
 4  $\{\{\}, \{3\}, \{2, 3\}, \{1\}\}$   
 5  $\{\{\}, \{3\}, \{2, 3\}, \{1, 3\}\}$   
 6  $\{\{\}, \{3\}, \{2\}, \{1, 2\}\}$   
 7  $\{\{\}, \{3\}, \{2\}, \{1, 2, 3\}\}$   
 8  $\{\{\}, \{3\}, \{2, 3\}, \{1, 2\}\}$   
 9  $\{\{\}, \{3\}, \{2, 3\}, \{1, 2, 3\}\}$   
 10  $\{\{\}, \{2\}, \{2, 3\}, \{1\}\}$   
 11  $\{\{\}, \{2\}, \{2, 3\}, \{1, 3\}\}$   
 12  $\{\{3\}, \{2\}, \{2, 3\}, \{1\}\}$   
 13  $\{\{3\}, \{2\}, \{2, 3\}, \{1, 3\}\}$   
 14  $\{\{\}, \{2\}, \{2, 3\}, \{1, 2\}\}$   
 15  $\{\{\}, \{2\}, \{2, 3\}, \{1, 2, 3\}\}$   
 16  $\{\{3\}, \{2\}, \{2, 3\}, \{1, 2\}\}$   
 17  $\{\{3\}, \{2\}, \{2, 3\}, \{1, 2, 3\}\}$   
 18  $\{\{\}\{3\}, \{1\}, \{1, 3\}\}$   
 19  $\{\{\}, \{3\}, \{1\}, \{1, 2\}\}$   
 20  $\{\{\}, \{3\}, \{1\}, \{1, 2, 3\}\}$   
 21  $\{\{\}, \{3\}, \{1, 3\}, \{1, 2\}\}$   
 22  $\{\{\}, \{3\}, \{1, 3\}, \{1, 2, 3\}\}$   
 23  $\{\{\}, \{2\}, \{1\}, \{1, 3\}\}$   
 24  $\{\{\}, \{2, 3\}, \{1\}, \{1, 3\}\}$   
 25  $\{\{3\}, \{2\}, \{1\}, \{1, 3\}\}$   
 26  $\{\{3\}, \{2, 3\}, \{1\}, \{1, 3\}\}$   
 27  $\{\{\}, \{2\}, \{1\}, \{1, 2\}\}$   
 28  $\{\{\}, \{2\}, \{1\}, \{1, 2, 3\}\}$   
 29  $\{\{\}, \{2\}, \{1, 3\}, \{1, 2\}\}$   
 30  $\{\{\}, \{2, 3\}, \{1\}, \{1, 2\}\}$   
 31  $\{\{\}, \{2, 3\}, \{1, 3\}, \{1, 2\}\}$   
 32  $\{\{\}, \{2, 3\}, \{1, 3\}, \{1, 2, 3\}\}$   
 33  $\{\{3\}, \{2\}, \{1\}, \{1, 2\}\}$   
 34  $\{\{3\}, \{2\}, \{1\}, \{1, 2, 3\}\}$   
 35  $\{\{3\}, \{2\}, \{1, 3\}, \{1, 2\}\}$

36  $\{\{3\}, \{2\}, \{1, 3\}, \{1, 2, 3\}\}$   
37  $\{\{3\}, \{2, 3\}, \{1\}, \{1, 2\}\}$   
38  $\{\{3\}, \{2, 3\}, \{1\}, \{1, 2, 3\}\}$   
39  $\{\{3\}, \{2, 3\}, \{1, 3\}, \{1, 2\}\}$   
40  $\{\{3\}, \{2, 3\}, \{1, 3\}, \{1, 2, 3\}\}$   
41  $\{\{\}, \{2\}, \{1, 2\}, \{1, 2, 3\}\}$   
42  $\{\{\}, \{2, 3\}, \{1, 2\}, \{1, 2, 3\}\}$   
43  $\{\{3\}, \{2\}, \{1, 2\}, \{1, 2, 3\}\}$   
44  $\{\{3\}, \{2, 3\}, \{1, 2\}, \{1, 2, 3\}\}$   
45  $\{\{2\}, \{2, 3\}, \{1\}, \{1, 3\}\}$   
46  $\{\{2\}, \{2, 3\}, \{1\}, \{1, 2\}\}$   
47  $\{\{2\}, \{2, 3\}, \{1\}, \{1, 2, 3\}\}$   
48  $\{\{2\}, \{2, 3\}, \{1, 3\}, \{1, 2\}\}$   
49  $\{\{2\}, \{2, 3\}, \{1, 3\}, \{1, 2, 3\}\}$   
50  $\{\{2\}, \{2, 3\}, \{1, 2\}, \{1, 2, 3\}\}$   
51  $\{\{\}, \{1\}, \{1, 3\}, \{1, 2\}\}$   
52  $\{\{\}, \{1\}, \{1, 3\}, \{1, 2, 3\}\}$   
53  $\{\{3\}, \{1\}, \{1, 3\}, \{1, 2\}\}$   
54  $\{\{3\}, \{1\}, \{1, 3\}, \{1, 2, 3\}\}$   
55  $\{\{\}, \{1\}, \{1, 2\}, \{1, 2, 3\}\}$   
56  $\{\{\}, \{1, 3\}, \{1, 2\}, \{1, 2, 3\}\}$   
57  $\{\{3\}, \{1\}, \{1, 2\}, \{1, 2, 3\}\}$   
58  $\{\{3\}, \{1, 3\}, \{1, 2\}, \{1, 2, 3\}\}$   
59  $\{\{2\}, \{1\}, \{1, 3\}, \{1, 2\}\}$   
60  $\{\{2\}, \{1\}, \{1, 3\}, \{1, 2, 3\}\}$   
61  $\{\{2, 3\}, \{1\}, \{1, 3\}, \{1, 2\}\}$   
62  $\{\{2, 3\}, \{1\}, \{1, 3\}, \{1, 2, 3\}\}$   
63  $\{\{2\}, \{1\}, \{1, 2\}, \{1, 2, 3\}\}$   
64  $\{\{2\}, \{1, 3\}, \{1, 2\}, \{1, 2, 3\}\}$   
65  $\{\{2, 3\}, \{1\}, \{1, 2\}, \{1, 2, 3\}\}$   
66  $\{\{2, 3\}, \{1, 3\}, \{1, 2\}, \{1, 2, 3\}\}$   
67  $\{\{1\}, \{1, 3\}, \{1, 2\}, \{1, 2, 3\}\}$

56 hypergraphs with 5 hyperedges:

1  $\{\{\}, \{3\}, \{2\}, \{2, 3\}, \{1\}\}$   
2  $\{\{\}, \{3\}, \{2\}, \{2, 3\}, \{1, 3\}\}$   
3  $\{\{\}, \{3\}, \{2\}, \{2, 3\}, \{1, 2\}\}$   
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21  $\{\{\}, \{2\}, \{2, 3\}, \{1, 3\}, \{1, 2\}\}$   
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 56  $\{\{2, 3\}, \{1\}, \{1, 3\}, \{1, 2\}, \{1, 2, 3\}\}$

28 hypergraphs with 6 hyperedges:

1  $\{\{\}, \{3\}, \{2\}, \{2, 3\}, \{1\}, \{1, 3\}\}$   
 2  $\{\{\}, \{3\}, \{2\}, \{2, 3\}, \{1\}, \{1, 2\}\}$   
 3  $\{\{\}, \{3\}, \{2\}, \{2, 3\}, \{1\}, \{1, 2, 3\}\}$   
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 15  $\{\{\}, \{2\}, \{2, 3\}, \{1\}, \{1, 3\}, \{1, 2\}\}$   
 16  $\{\{\}, \{2\}, \{2, 3\}, \{1\}, \{1, 3\}, \{1, 2, 3\}\}$

17  $\{\{3\}, \{2\}, \{2,3\}, \{1\}, \{1,3\}, \{1,2\}\}$   
18  $\{\{3\}, \{2\}, \{2,3\}, \{1\}, \{1,3\}, \{1,2,3\}\}$   
19  $\{\{\}, \{2\}, \{2,3\}, \{1\}, \{1,2\}, \{1,2,3\}\}$   
20  $\{\{\}, \{2\}, \{2,3\}, \{1,3\}, \{1,2\}, \{1,2,3\}\}$   
21  $\{\{3\}, \{2\}, \{2,3\}, \{1\}, \{1,2\}, \{1,2,3\}\}$   
22  $\{\{3\}, \{2\}, \{2,3\}, \{1,3\}, \{1,2\}, \{1,2,3\}\}$   
23  $\{\{\}, \{3\}, \{1\}, \{1,3\}, \{1,2\}, \{1,2,3\}\}$   
24  $\{\{\}, \{2\}, \{1\}, \{1,3\}, \{1,2\}, \{1,2,3\}\}$   
25  $\{\{\}, \{2,3\}, \{1\}, \{1,3\}, \{1,2\}, \{1,2,3\}\}$   
26  $\{\{3\}, \{2\}, \{1\}, \{1,3\}, \{1,2\}, \{1,2,3\}\}$   
27  $\{\{3\}, \{2,3\}, \{1\}, \{1,3\}, \{1,2\}, \{1,2,3\}\}$   
28  $\{\{2\}, \{2,3\}, \{1\}, \{1,3\}, \{1,2\}, \{1,2,3\}\}$

8 hypergraphs with 7 hyperedges:

1  $\{\{\}, \{3\}, \{2\}, \{2,3\}, \{1\}, \{1,3\}, \{1,2\}\}$   
2  $\{\{\}, \{3\}, \{2\}, \{2,3\}, \{1\}, \{1,3\}, \{1,2,3\}\}$   
3  $\{\{\}, \{3\}, \{2\}, \{2,3\}, \{1\}, \{1,2\}, \{1,2,3\}\}$   
4  $\{\{\}, \{3\}, \{2\}, \{2,3\}, \{1,3\}, \{1,2\}, \{1,2,3\}\}$   
5  $\{\{\}, \{3\}, \{2\}, \{1\}, \{1,3\}, \{1,2\}, \{1,2,3\}\}$   
6  $\{\{\}, \{3\}, \{2,3\}, \{1\}, \{1,3\}, \{1,2\}, \{1,2,3\}\}$   
7  $\{\{\}, \{2\}, \{2,3\}, \{1\}, \{1,3\}, \{1,2\}, \{1,2,3\}\}$   
8  $\{\{3\}, \{2\}, \{2,3\}, \{1\}, \{1,3\}, \{1,2\}, \{1,2,3\}\}$

1 hypergraph with 8 hyperedges:

1  $\{\{\}, \{3\}, \{2\}, \{2,3\}, \{1\}, \{1,3\}, \{1,2\}, \{1,2,3\}\}$