PARA-FIBONACGI SEQ ETC Budl A19586 A19594 A35336 ff A26351,5 A201 3

OR equivales

Bud 2

052413

m < n St.

[mc] < { = 100 = 3

Linear Predictive Coder (RPE-LPC) with a Long Term A Copy Basically, inform on previous samples, which does not change very quickly, is used to redict the current sample coefficients of the linear combination of the previous samples, we are encoded form of sidual, the difference between the predicted and actual sample, represent the signal. Spec

livided into 20 millisecond samples, each of which is encoded as 260 lits, giving a total bit rate of

01

bed 3 6 20941 23 3/ (nz)+2 26351 = [nT]+1 201 = [17]

From njas Fri Nov 22 10:31 EST 1996

To: ck6@cedar.evansville.edu Cc: njas@research.att.com

hi! some time ago you sent me a paper with the following sequence in it:

%I A003603 M0138

%S A003603 1,1,1,2,1,3,2,1,4,3,2,5,1,6,4,3,7,2,8,5,1,9,6,4,10,3,11,7,2,12,8,5,13,1,

%T A003603 14,9,6,15,4,16,10,3,17,11,7,18,2,19,12,8,20,5,21,13,1,22,14,9,23,6,24

%N A003603 Fractal sequence obtained from Fibonacci numbers.

%R A003603 Kimb94a.

%O A003603 0,4

%A A003603 njas, mb

%K A003603

john conway recently rediscovered this sequence, so i am writing to ask if that paper of yours

[Kimb94a] = C. Kimberling, ''Numeration systems and fractal sequences,'' preprint, 1994.

has appeared? and if you could send me another copy, of either the original form or the published version?

thanks!

PS here is jhc's version:

%I A019586

%S A019586 0,0,0,1,0,2,1,0,3,2,1,4,0,5,3,2,6,1,7,4,0,8,5,3,9,2,10,6,1,11,7,4,

%T A019586 12,0,13,8,5,14,3,15,9,2,16,10,6,29,1,30,11,7,19,4,20,12,0,21,13,8,

%U A019586 22,5

%N A019586 Takes value i on later (i.e. b_j, j>=2) terms of ith Fibonacci sequence defin

%R A019586 jhc.

%K A019586 nonn

%O A019586 1.6

%A A019586 njas, jhc

Neil Sloane, njas@research.att.com, fax: 908 582 2379 AT&T Research Labs, Room 2C-376, 600 Mountain Ave, Murray Hill, NJ 07974 USA Home page: http://netlib.bell-labs.com/math/sloane/doc/home.html

From cedar.evansville.edu!ck6 Fri Nov 22 11:02 EST 1996

(Smail3.1.29.1 #13) id m0vQy0Z-0002fJC; Fri, 22 Nov 96 09:59 CST

Date: Fri, 22 Nov 1996 10:01:56 -0500 (cst)

From: Clark Kimberling <ck6@cedar.evansville.edu>

To: njas@research.att.com

In-Reply-To: <m0vQxeA-0002fXC@evansville.edu>

Neil,

The paper appeared in Acta Arithmetica 73 (1995) 103-117. I'll send you a copy. (What was the context of John's work that led him to this

sequence?)

From and.Princeton.EDU!conway Sat Nov 23 13:59 EST 1996

Return-Path: <conway>

Date: Sat, 23 Nov 1996 13:43:37 -0500 (EST)
From: John Conway <conway@math.Princeton.EDU>

Subject: Re: parFibs.
To: njas@research.att.com

In-Reply-To: <199611221536.KAA28194@and.Princeton.EDU>

Will you please put the name "para-Fibonacci sequence" in the entry for my version? Correspondingly, perhaps something like "Fibonacci paraphrase" should be in Kimberling's.

I've been continuing my study of these matters, and thinking about the terminology, the most important new pieces of which are the word "parameter" for the index of a sequence, and (Fibonacci) "successor" for the number Sn you get from a given n by bumping up all terms of its Zeckendorff expansion. Thus the sequence with parameter i can be started from

i 1+Si

and after that has the shape

j sj ssj sssj ssssj ...

where j = i + 1 + Si.

On Fri, 22 Nov 1996 njas@research.att.com wrote:

- > >From njas Fri Nov 22 10:31 EST 1996
- > To: ck6@cedar.evansville.edu
- > Cc: njas@research.att.com
- > Status: R
- > hi! some time ago you sent me a paper with the following sequence in it:
- > %I A003603 M0138
- > %S A003603 1,1,1,2,1,3,2,1,4,3,2,5,1,6,4,3,7,2,8,5,1,9,6,4,10,3,11,7,2,12,8,5,13,1,
- > %T A003603 14,9,6,15,4,16,10,3,17,11,7,18,2,19,12,8,20,5,21,13,1,22,14,9,23,6,24
- > %N A003603 Fractal sequence obtained from Fibonacci numbers.
- > %R A003603 Kimb94a.
- > %O A003603 0,4

From netcom.com!hbaker Sat Nov 23 14:44 EST 1996

From: hbaker@netcom.com (Henry G. Baker)

Subject: M1,398,269

To: math-fun@cs.arizona.edu

Date: Sat, 23 Nov 1996 11:38:07 -0800 (PST)

Move over, supercomputers

From cs.arizona.edu!rcs Mon Nov 25 16:29 EST 1996

Date: Mon, 25 Nov 1996 14:20:11 MST

From: "Richard Schroeppel" <rcs@cs.arizona.edu>

To: math-fun@cs.arizona.edu

Subject: Fibonacci note from Conway

This came up on another list. I think it's of more interest here on Math-Fun. My apologies to the common membership for a double-post. --Rich

From: John Conway <conway@math.Princeton.EDU> Subject: Re: Fibonacci correction from Achim Date: Mon, 25 Nov 1996 12:51:57 -0500 (EST)

This mention of Fibonacci counting prompts me to pass on something about the Fibonacci's that very much excited me when I found it about a week ago. I've since learned that Clark Kimberling found the essential point about 20 years ago.

I start with the Zeckendorff expansion of a positive integer, obtained by repeatedly subtracting the largest Fibonacci number you can until nothing remains, for example

$$100 = 89 + 8 + 3$$
.

By replacing each Fib in the Zeckendorff expansion of n, you get what I'll call the Fibonacci successor Sn, eg.:

$$S100 = 144 + 13 + 5 = 162$$
.

Now the positive integers are linked by this function into an infinity of sequences each satisfying the Fibonacci recursion, namely those after the bar in the table below, which covers all numbers below 100:

```
0 1 1 2 3 5 8 13 21 34 55 89
1 3 4 7 11 18 29 47 76
   4 | 6 10 16 26 42 68
 3 6 9 15 24 39 63
    8 | 12 20 32 52 84
5 9 14 23 37 60 97
 6 11 17 28 45 73
  7 12 19 31 50 81
 8 14 22 36 58 94
 9 16 25 41 66
 10 17 27 44 71
 11 19 30 49 79
 12 21 33 54 87
 13 22 35 57 92
 14 24 38 62
 15 25 40 65
 16 27 43 70
 17 29 46 75
 18 30 48 78
 19 32 51 83
```

20 33 | 53 86 21 35 | 56 91 22 37 | 59 96 23 38 61 99 24 40 64 25 42 67 26 43 69 27 45 72 28 46 74 29 48 77 30 50 80 31 51 82 32 53 85 33 55 88 34 56 90 38 63 |

The topmost series is the Fibonacci series itself: I call the n'th one beneath it the n'th extra Fibonacci sequence. It occurs to me that "n'th higher Fibonacci sequence" might be better. The 0'th higher Fib sequence is of course the Fib sequence itself.

Of course each of these sequences can be continued indefinitely far to the left, and I continued them two places left in the table, because then, as you can see, the leftmost column contains the parameter n just defined.

It's a very nice fact that EVERY sequence that satisfies the Fibonacci recurrence and ends up with positive integers is one of this neatly-parameterized family. This leads us to what I call the "para-Fibonacci sequence), which for every positive integer gives the parameter of the Fib-sequence that contains that integer (after the bar):

0 0 0 1 0 2 1 0 3 2 1 4 0 5 3 2 6 1 7 4 0 8 5 3 9 2 10 6 1 11 7 4 12 0 13

Kimberling called the sequence whose terms are 1 larger than these "the paraphrase of the Fibonnaci numeration system".

This has very nice properties - for example between any two $\[N \]$ 0's we see a permutation of the first few positive integers, and these nest, so we can read the paraFib sequence from:

Also - if you delete the first occurrence of each number, the sequence is unchanged.

There are many intriguing problems here, of which I'll mention just two:

- 1) Reading the nth sequence backwards, we obtain the negative of another. Which?
- 2) Multiplying the terms of the nth sequence by some positive integer d, we obtain those of another. Which? (The reason I prefer my version to Kimberling's is that the answer to this must be some multiple of d.)
- I only just thought of 1). About 2) I note that multiplying the Fib sequence by 2,3,4, 5, 6, 7, 8, 9,10,11 we get sequences numbers 2 3 4 15 18 21 24 27 30 33,

and that the double of the 7th sequence comes before that of the 5th.

I have long been interested in what I call the "budding sequences", which tell you where the successive buds on suitable kinds of plant are located. The paraFib sequence helps to explain many properties of these, and shows that they each consist of the terms of the rather mysterious sequence

1, 3, 2, 5, 8, 5, 9, 5, 10, 15, 9, 15, 21, 13, 20, ...

repeated infinitely often in systematic ways. However, to explain these matters here would take me as much time again, and I want to have some lunch now!

John Conway