





FACULTY OF ARTS AND SCIENCE / DEPARTMENT OF MATHEMATICS, STATISTICS AND COMPUTING SCIENCE

July 30, 1970

Neil J.A. Sloane
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Dear Neil,

A brief reply as I am far behind with correspondence, having just returned from sabbattical.

Many thanks for the 4th(?) edition of Sequences and your kind acknowledgement. Thanks too for your letter of 22-24:7:70 and the corrections to research paper #9.

#9 was a "reprint" of Richard K. Guy, Dissecting a polygon into triangles, Note 90, Bull. Malayan Math. Soc. 5(1958), 57-60. It was only later I realized that  $D_n$  were the Catalan numbers. The originality was in the  $E_n$  calculation.

#11, "A theorem in partitions" was submitted to JLMS after Davenport, Rogers and Hansraj Gupta told me they thought it to be original, but the theorem turned out to be due to Glaisher. Some of the proofs were perhaps new, but I haven't attempted to publish it elsewhere.

#33, "The no-3-in-line problem". See Guy, R.K. and Kelly, P.A.,
The no-three-in-line problem, Canad. Math. Bull., 11(1968), 527-531.
Also AMS Notices, 15(1968), 550. M.R. 39(1970), #129. Also, in Tutte, ~ Note:
W.T. (editor) Recent Progress in Combinatorics, Academic Press, New
York, 1969, page 337.

#8, "The crossing number of the complete graph" is a "reprint" of Guy, R.K., A combinatorial problem, Bull. Malayan Math. Soc., 7(1960), 68-72. (BMMS did not do offprints and had a very small and almost entirely local circulation). There is still a lot of mythology on this topic, but I now claim to have a sound proof (the first!) that  $\nu(K_n)$  is what we conjecture it is for  $n \leq 10$ . I hope that a student, Roger B. Eggleton, and I can soon extend this to n=12. I have also proved that  $\bar{\nu}(K_n)$ , the rectilinear crossing number, =  $\nu(K_n)$  for  $n \leq 7$ , n=9 and that  $\bar{\nu}(K_8)=19$ . I think I can soon show  $\bar{\nu}(K_{10})=63$ . Papers will appear in the Proc. of the recent St. John's Univ. Conference and perhaps (with Eggleton) in J. Combinatorial Theory.

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For the coarseness of the complete graph and complete bipartite graphs, see papers in Can. J. Math. 20(1968), 888-894 MR 37(1969), 1086-1096. Beineke and I have not tried to close the small gaps. We are currently looking at the coarseness of  $Q_n$ , the n-cube, but we may have to leave gaps there, too.  $c(Q_n) = 0$  for  $n \le 3$ ,  $c(Q_4) = 2$ ,  $c(Q_5) = 4$  or 5, almost certainly the former.  $10 \le c(Q_6) \le 13$ , can probably prove  $\le 12$  and believe 10. Generally

$$\left[\frac{n}{4}\right]2^{n-3} \leq c(Q_n) \leq \left[n2^{n-2}/7\right]$$

but we hope to improve both bounds.

Have seen Conway and Mike Guy since we last met. Can assure you they appreciate Sequences even if they haven't acknowledged.

Haven't yet seen Kenyon since I got back. Will leave a note reminding him to send a copy of thesis. Maybe I forgot to ask him; he is usually good about such things.

Glad to know your list has proved useful. I was sure it would be: I discussed such a project with Leo Moser some years ago. Met Knuth (again) in Stanford recently. Selfridge was giving a talk and I was travelling from Santa Cruz to Berkeley, so gave him a ride. Knuth was disappointed I was not Mike Guy as he wanted to discuss some work Mike had done with Conway.

Will try to write more if ever I get rid of the piles of paper. Best wishes to Graham, Gilbert, Berlekamp, Knowlton, Pollak, et al.

Yours sincerely,

Richard K. Guy

RKG/vh





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July 30, 1971.

Dr. N. J. A. Sloane, Bell Laboratories, 600 Mountain Avenue, Murray Hill, New Jersey, 07974, U.S.A.

Dear Neil,

Glad to hear you on the phone.

I am sending a copy of "The no-3-in-line problem" by separate mail. You will see line 10 has been added. If you have an original copy (not the Canad. Bull. version, but the Calgary preprint), then just add to the bottom of the table:

10 3 1 - 132 13 1 6 156 1135 4448

 $$\operatorname{Send}$  a copy of "A poke at a problem in the previous paper" if you get it into shape.

I am also sending a copy of "the nesting and roosting habits of the laddered parenthesis" which contains a plug for your book.

All the best to Ron, Elwyn, Jessie, Jack,.... We also remember Klarner.

Sincerely,

Richard K. Guy.

RKG:1h

Encl.

Solve of Sedlaceh!



## **Bell Laboratories**

600 Mountain Avenue Murray Hill, New Jersey 07974 Phone (201) 582-3000

August 2, 1971

Prof. P. A. Kelly Department of Combinatorics University of Waterloo Waterloo, Ontario CANADA

Dear Professor Kelly:

In 1968 Richard Guy told me the answers to the no-three-in-line problem for n  $\leq$  9:

009	k	n	2	3	4	5	6	7	8	9	10	//
100	7/9/2	S	1	1	4	5	11	22	57	51	156	po for.
10	76(0)	Т	1	2	11	32	50	132	380	368	1135	
73	15)	t	0	8	44	152	372	824	1544	2712	4448	
175	n 2 3 4 5 6 7 8 9 10  769 s 1 1 4 5 11 22 57 51 156  755 T 1 2 11 32 50 132 380 368 1/35  7 55 T 0 8 44 152 372 824 1544 2712 4448											

Could you please tell me if any further terms are known in any of these sequences? Thank you very much.

Yours sincerely,

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Veil Stoane

N. J. A. Sloane

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Enclosed are two papers on this topic. If you would like the actual configurations please drops me a line. at present I am finishing a paper on the generalization of this problem to an mxm grid

Sinurely Patrick a T. Kelly.